## FORM FOUR CLUSTER KCSE MODEL10

## MATHEMATICS PAPER 2 QUESTIONS

## SECTION I (50 Marks)

## (Answer all the questions in this section.)

1. Without using logarithm tables or calculator solve

$$
\log 5-2+\log (2 x+10)=\log (x-4)
$$

2. Make $p$ the subject of the formula

$$
\frac{y}{r}=\frac{a}{p n}+\frac{b}{a p}
$$

3. Find the percentage error in estimating the volume of a cone whose radius is 3.2 cm and height is 8 cm .
4. Find the equation of a circle whose centre is

$$
\left(\frac{1}{2}, \frac{-2}{3}\right) \text { and radius is } 3 \text { units leaving your answer }
$$

in the form $a x^{2}+b y^{2}+c x+d y+c=0$ where $a, b, c, d$ and $e$ are integers. (3marks)
5. Water and milk are mixed such that the ratio of the volume of water to that of milk is $3: 2$. Taking the density of water as $1 \mathrm{~g} / \mathrm{cm} 3$ and that of milk as $1.2 \mathrm{~g} / \mathrm{cm} 3$, find the mass in grams of 2.5 litres of the mixture.
6. Solve $5 \operatorname{Sin}^{2} x+\operatorname{Sin} x-4=0$
hence find Tan $x$ and $\operatorname{Cos} x$ if $x$ is an obtuse angle.
7. Expand $(1-1 / 2 x)^{5}$ up to the term in $x 3$, hence use your expansion to evaluate
8. In the figure below, $D C=6 \mathrm{~cm} A B=5 \mathrm{~cm}$. Determine $B C$ if $D C$ in stonment

9. Find the values of $x$ for which is a singular matrix.
10. Simplify

$$
\frac{2}{2-\sqrt{3}}-\frac{3}{3-\sqrt{3}}
$$

$$
\text { leaving your answer in the form of } a+b \sqrt{c}
$$

11. Evaluate using logarithm tables.

## $\left\{\frac{\log 8293}{0.456 \tan 81.2^{\circ}}\right\}^{2 / 3}$

12. The starting salary of Nasirembe per annum is $£ 8040$, His salary increased at the end of each year by $12 \%$. Determine his earning per month during the 7th year.
13. The variable $R$ varies partly as a constant and partly inversely as the square root of $Z$. When $R=11$, $Z=36$, when $R=22, Z=1 / 4$. Write an equation connecting $R$ and $Z$.
14. Find the length represented by $Y$ in the figurebelow.

15. Kuloba bought a jembe at $12 \%$ discount. After using it for a while she sold it at sh 211.20 which was $80 \%$ of its buying price. Find the marked price of the jembe before discount.
16. The figure below represents the linear equation

$$
\log y=n \log x+\log k
$$

. Use the graph to find the value of $n$ and $k$.

a) Use the graph to find the values of $n$ and $k$.

## SECTION II (50 Marks)

## Answer ONLY FIVE questions in this section)

17. A cylindrical water tank can be filled to a depth of 2.1 m by a pipe $A$ in 2 hours pipe $B$ takes 7 hours to fill the tank to the same depth. Pipe C can empty this amount in 6 hours. a) i) Starting with the empty tank and pipe A running for one hour, find the depth of water after one hour. (2marks)
ii) If pipe $A$ is turned off and pipe $C$ is left open for one hour find the depth of water. (2marks)
b) If the tank is initially empty and pipe $A$ and $B$ are both running while pipe $C$ is left open, after how long will the depth of water reach 2 m . (3marks)
c) 25 men working 8 hours a day plant trees in a forest plot in 63 days. Calculate the number of days 45 men working 7 hours a day would take to plant the same number of trees (Assume that all the men work at the same rate) (3marks)
18. A car whose initial value is kshs. 600000 depreciates at a rate of $12 \%$ p.a. Determine a) Its value after 5 years. (4marks)
b) The value of depreciation after 5 years. (2marks)
c) The number of years it will take for the value of the car to be Kshs. 300 000. (4marks)
19. The marks scored by 50 students in a math test were as shown below.

| Marks | $10-19$ | $20-29$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ | $90-99$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 1 | 2 | 5 | 8 | 13 | 10 | 6 | 3 | 2 |

a) State the modal class. (1mark)
b) On the grid provided draw an O give of the above data. (3marks)

c) From the graph determine i) The median mark. (1mark)
ii) The Quartile deviation. (3marks)
iii) The pass mark if $44 \%$ of the students passed the test. (2marks)
20. The figure below $P, Q, R$ and $S$ are points on the circle centre $O$. PRT and USTV are straight lines. Line UV is a tangent to the circle at S. $<$ RST $=50^{\circ}$ and $\angle R T V=150^{\circ}$

a) Calculate the size of the following angles giving reasons
i) <ORS (2marks)
ii) <USP (2marks)
iii) <PQR (2marks)

Given that $\mathrm{RT}=7 \mathrm{~cm}$ and $\mathrm{ST}=9 \mathrm{~cm}$. Calculate to 4 significant figures i ) The length of the line PR (2marks)
ii) The radius of the circle (2marks)

2L. In the figure below ABCD is a parallelogram such that $A B=a \quad B C=b \quad A E: E B=3: 1, \mathrm{X}$ is the intersection of $D E$ and $A C$.

a) Write in terms of $a$ and $b$ the vectors
i) $A C$
(Imark)
i) $D E$
(1mark)
b) $A X-k A C, D X-n D E$, $A X-A D+D X$

Find the values of $n$ and $k$.
(6marks)
21. . Complete the table below for the functions

| x | $0^{\circ}$ | $30^{\circ}$ | $60^{\circ}$ | 90 | 120 | 150 | 180 | 210 | 240 | 270 | 300 | 330 | 360 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $2 \operatorname{Sin}\left(\mathrm{x}-30^{\prime \prime}\right)$ | -1 |  |  | 1.73 | 2 |  |  | 0 | -1 |  |  | -1.73 |  |
| $\operatorname{Cos} 2 \mathrm{x}$ | 1 |  |  | -1 | -0.5 |  |  | 0.5 | -0.5 |  |  | 0.5 |  |

a) On the same set of axes, draw the graphs of $v=2 \operatorname{Sin}\left(x-30^{\circ}\right)$ and $v=\operatorname{Cos} 2 x$
in the range $r \times x \times m$

b) Use your graph to solve the equation $2 \operatorname{Sin}\left(x-30^{\circ}\right)=\operatorname{Cos} 2 x$
(1mark)
c) State the;
i) Phase angle for the wave
$y=2 \sin \left(x-30^{\circ}\right)$
(1 Mark)
ii) Period for the wave

$$
y=\operatorname{Cos} 2 x
$$

(l mark)
22. . Bag A contains 2 red balls and 3 blue balls Bag B contains 4 red balls and 5 blue balls. Two balls are drawn at random from bag $A$ and placed in Bag $B$ and then a ball is drawn at random from $B$.

a) Complete the tree diagram. (4marks)
b) What is the probability that i) All the three balls drawn are of the same colour? (2marks)
ii) The ball from bag $B$ is blue. (4marks)
23. a) A plane takes off from airport $P$ at $\left(0^{\circ}, 40^{\circ} \mathrm{W}\right)$ and flies 1800 nautical miles due East to $Q$ then 1800 nautical miles due South to R and finally 1800 nautical miles due west before landing at S . a) Find to the nearest degree the locations of $\mathrm{Q}, \mathrm{R}$ and S . (4marks)
b) If the total flight time is 16 hours, find the average speed in knots for the whole journey. (3marks)
c) Find the time taken to fly from R to S, given that this was two hours shorter than the time taken P and Q to R. (3marks)

