## STAREHE BOYS HIGH SCHOOL MOCK 2015

## MATHEMATICS PAPER 2

## Section I- (50 marks). Answer all questions

1) Use logarithm tables to solve

$$
\left(\frac{2.925 \times 0.0784}{\log 432.4}\right)^{\frac{-2}{3}}
$$

2) a. Expand and simplify $\left(\frac{1}{2} x-\frac{1}{3} y\right)^{4}$

2marks
b. Hence evaluate $\left(\frac{1}{\sqrt{2}}-\frac{1}{\sqrt{3}}\right)^{4}$ leaving your answer in surd form $\quad 2$ marks
3) A mixture is made by mixing 4 kg of long grain rice costing sh 60 per kg with 9 kg of short grain rice costing sh 50 per kg. How many kilograms of long grain rice should be added to the mixture so that the resulting mixture can be sold at sh 66 per kg and a profit of $20 \%$ is made. 3marks
4) Find the centre and radius of a circle whose equation is $2 x^{2}+2 y^{2}-12 y-14=0$ 3marks
5) Peter invested a certain amount of money in a financial institution at compound interest compounded quarterly. At the end of the third year it had amounted to sh 18980 and by the end of the fifth year it had amounted to sh 20530. Find the rate of interest

4marks
6) A point C divides the line AB with coordinates $\mathrm{A}(3,4,-5), \mathrm{B}(-1,10,7)$ externally in the ratio $5: 3$. Find the coordinates of C 3marks
7) A and B are points on latitude $70^{\circ} \mathrm{N}$. Their longitudes are $62^{\circ} \mathrm{W}$ and $118^{\circ} \mathrm{E}$ respectively. Find the shortest distance between $A$ and $B$ in nautical miles.

## 2marks

8) Estimate the area enclosed by the curve $\boldsymbol{y}=\frac{\mathbf{1}}{\mathbf{4 x + 1}}$ and the $x$ axis from $x=0$ to $x=2$ using mid ordinate rule with four strips. (Leave your answer as a fraction).

3marks
9) In the figure below $A B$ and $C D$ are chords intersecting internally at point $X$. If $\mathrm{CD}=6.5 \mathrm{~cm}, \mathrm{CX}=2.5 \mathrm{~cm}$ and $\mathrm{BX}=2.2 \mathrm{~cm}$ Calculate the length of AX .

10) Calculate the standard deviation of the given data
11) Make $C$ the subject of a formula in the equation

$$
v^{2}=\frac{r}{3}+\sqrt{\frac{1+c^{2}}{r^{2}}}
$$

12) The forth term of a geometric sequence is 48 and the seventh term is 384 .Find the common ratio and the ninth term of the sequence.

3marks
13) The masses of two objects to the nearest 100 g are 51 kg , and 43 kg find the percentage error in the difference of their masses.

3marks
14) Solve the equation $9 \tan ^{2} \theta+\tan \theta=10$ for $0^{0} \leq \theta \leq 360^{\circ}$

4marks
15) The volume $V$ of a cylinder varies jointly as the square of the radius $R$ and the height $H$. If the radius is increased by $10 \%$ and the height decreased by $20 \%$ find the percentage change in the volume.

3marks
16) a. Determine the inverse of the matrix $T=\left(\begin{array}{rr}1 & 2 \\ 1 & -1\end{array}\right) \quad 1$ mark
b. Hence find the co-ordinates of the point of intersection of the lines whose equation are $x+2 y=7$ and $x-y=1$

2marks

## SECTION II - (50 MARKS).

Answer ONLY five questions
17. a. AB and CD are chords of a circle Construct the circle with centre O and measure its radius 4marks

b. Construct the loci of a points $x$ which are equidistant from line $A B$ and $C D$ 1mark
c. locate the loci of a points $Y$ which are equidistant from points $C$ and $D$ 1mark

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d. Construct the loci of a points $Z$ which are 2 cm from the circumference of the circle.

1marks
e. A point $P$ moves such that $C P \geq D P$, It is not more than 2 cm from the circumference of the circle and its distance from line $C D$ is not more than its distance from $A B$. Show the region $P$ by shading it.

3marks
18)a. Complete the table below, giving values correct to two decimal places.

| $x^{0}$ | 0 | 15 | 30 | 45 | 60 | 75 | 90 | 105 | 120 | 135 | 150 | 165 | 180 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\operatorname{Tan} x^{0}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $2 \sin 2 x^{0}-2$ |  |  |  |  |  |  |  |  |  |  |  |  |  |

b. Draw the graph of $y=\tan x^{0}$ and $y=2 \sin 2 x^{0}-2$
c. From your graph state the amplitude and period of $y=2 \sin 2 x^{0}-2$

1mark
d. Use your graph to solve the equation
i. $\frac{1}{2} \tan x^{0}+1=\sin 2 x^{0}$
ii. $\sin 2 x^{0}=0$

1mark

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19 In order to ensure optimal health a lab technician needs to feed the rabbits on a daily diet containing a minimum of 24 grams of fat, 36 grams of carbohydrates and 4 grams of protein. Rather than order rabbit food that is custom blended it is cheaper to order food X and food Y and blend them for an optimal use. One packet of food X contains 6 grams of fat , 12 grams of carbohydrates, 2 grams of proteins and costs Sh 50.While one packet of food Y contains 12grams of fat, 12 grams of carbohydrates, 1 gram of proteins and it costs Sh 60
a. Form all the inequalities to represent the information above.

4marks
b. Graph the inequalities

4marks
c. Determine the number of packets of type X and Y feed that should be used for optimal health at minimum cost.

2marks
20. The diagram below shows the frustum of a rectangular based pyramid. The base ABCD is a rectangle of side 24 cm by 12 cm . The top EFGH is a rectangle of side 14 cm by 7 cm .Each of the slanting edges of the frustum is 13 cm .


Determine the
a. altitude of the frustum

4marks
b. angle between the line AG and the base ABCD

3marks
c. Volume of the frustum

3marks

20 At the Kenya medical research institute a new drug is being tried. A sample of eighty sick rats is being used. Sixty of these rats are given drugs and the rest are not. A half of those given drugs are put on a high calorie diet while three quarters of those who are not given drugs were put on the same diet. For the ones who are treated and put on a high calorie diet the probability of dying is 0.1 and 0.2 if not put on a high calorie diet. For the ones who are not treated and put on a high calorie diet the probability of dying is 0.4 and 0.6 if not put on a high calorie diet.
a. Draw a tree diagram to represent the above information.

2marks
b. Calculate the probability that a rat picked at random
i. Is given drugs, put on a high calorie diet and will die 1mark
ii. Is given drugs and will die . 2marks
iii. Will die

3marks
iv. Is not given drugs and will not die

2marks
21. The table below shows the rate at which income tax was charged for all income earned in the year 2012

| Taxable income per month in $\mathrm{k} £$ | Rate of tax per $\mathrm{k} £$ |
| :---: | :---: |
| $1-236$ | $10 \%$ |
| $237-472$ | $15 \%$ |
| $473-708$ | $20 \%$ |
| $709-944$ | $25 \%$ |
| 945 and above | $30 \%$ |

a. A tax of ksh1200 was deducted from Mr. Rono's monthly salary. He was entitled to a personal relief of ksh 1064 per month. Calculate his monthly
i. Gross tax in $\mathrm{k} £$.

1mark
ii. Taxable income in ksh

5marks
b. He was entitled to a house allowance of ksh 3000 and medical allowances of ksh 2000 calculate his monthly basic salary in ksh.

1mark
c. Every month the following deductions were made from his salary electricity bill of sh 680 , water bill of sh 460 , co-operative shares of sh 1250 and loan repayment of sh 2000 calculate his net salary in ksh.

3marks
23. A particle is moving with an acceleration of $(t-4) \mathrm{m} / \mathrm{s}^{2}$ where t is time in seconds. When t is 2 seconds the velocity is $4 \mathrm{~m} / \mathrm{s}$ and when t is 0 the displacement is 0 m
a. Express velocity in terms of t

2marks
b. Find the displacement of the particle during the third second. 2marks
c. Calculate the interval of time when the velocity was not more than $4 \mathrm{~m} / \mathrm{s}$

3marks
d. Calculate the minimum velocity.

3marks
24. In the figure below $O$ is the centre of the circle and $A B C D E A$ is a regular polygon inscribed in a circle. Line GEF is a tangent to the circle at point E

e. Find angle
i. AEG 1marks
ii. OEC

2marks
iii. DFE

2marks
iv. Obtuse angle AOC 2marks
f. If the sides of the pentagon are 6 cm find the area of the circle giving your answer to one decimal place

